Orange Public Schools

Office of Curriculum & Instruction 2019-2020 Mathematics Curriculum Guide



Second Grade Mathematics

Unit 2: Eureka - Module 2: Add/ Subtract Length September 30, 2019 – October 18, 2019

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Yearlong Pacing Guide: Second Grade

Eureka Math	Eureka Module Standards
Unit 1- Module 1: Sum/ Difference to 20 Sept 9- Sept 27	20A1, 20A2, 2NBT5
Unit 2-Module 2: Add/ Subtract Length Sept 30- Oct 18	2MD1, 2MD2, 2MD3, 2MD4, 2MD5,2MD6
Unit 3- Module 3: Place Value, Count to 1000 Oct 21 – Nov 26	2NBT1, 2NBT2, 2NBT3, 2NBT4
Unit 4- Module 4: Add/ Subtract within 200 (Word Problems up to 100) Dec 2- Jan 31	20A1, 2NBT5, 2NBT6, 2NBT7. 2NBT8, 2NBT9
Unit 5- Module 5: Add/ Subtract within 1000 (Word Problems up to 100) Feb 3- March 13	<mark>2NBT7, 2NBT8, 2NBT9</mark>
Unit 6- Module 7: Length, Money, Data March 16- May 8	2NBT5, 2MD1, 2MD2, 2MD3, 2MD4, 2MD5, 2MD6, <mark>2MD8, 2MD9, 2MD10</mark>
Unit 7- Module 8: Time, Shapes, Fractions May 11- June 5	<mark>2MD7, </mark> 2G1, 2G3
Unit 8- Module 6: Foundations Multiplication Division June 8- EOSY	<mark>20A3, 20A4</mark> , <mark>2G2</mark>

References

"Eureka Math" Gt Minds. 2018 < https://greatminds.org/account/product

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Mod	lule 2
Essential Questions	Enduring Understandings
 What units and tools measure the different attributes? Why are standard units of measurement used? Why are units used in measuring? How are perimeter and area different? How does estimation help us with measurement? 	 Specific tools measure specific attributes. A measurement must contain a number and a unit. The significance of numbers affects the outcome of operations on them.

Performance Overview

- Topic A opens with students exploring concepts related to the centimeter ruler. In the first lesson, they are guided to connect measurement with physical units as they find the total number of length units by laying multiple copies of centimeter cubes (physical units) end to end along various objects. Through this, students discover that to get an accurate measurement, there must be no gaps or overlaps between consecutive length units. Next, students measure by iterating with one physical unit, using the mark and advance technique, also known as mark and move forward. Students then repeat the process by laying both multiple copies and a single cube along a centimeter ruler. This helps students create a mental benchmark for the centimeter. It also helps them realize that the distance between 0 and 1 on the ruler indicates the amount of space already covered. Hence 0, not 1, marks the beginning of the total length. Students use this understanding to create their own centimeter rulers using a centimeter cube and the mark and advance technique. Topic A ends with students using their unit rulers to measure lengths, thereby connecting measurement with a ruler. Students build skill in measuring using centimeter rulers and meter sticks
- In Topic B, students learn to see that a length unit is not a cube, or a portion of a ruler (which has width) but is a segment of a line. By measuring a variety of objects, students build a bank of known measurements or benchmark lengths, such as a doorknob being a meter from the floor, or the width of a finger being a centimeter. Students learn to estimate length using knowledge of previously measured objects and benchmarks. This enables students to internalize the mental rulers of a centimeter or meter, empowering them to mentally iterate units relevant to measuring a given length. The knowledge and experience signal that students are determining which tool is appropriate to make certain measurements
- In Topic C, students measure and compare to determine how much longer one object is than another. They also
 measure objects twice using different length units, both standard and non-standard, thereby developing their
 understanding of how the total measurement relates to the size of the length unit. Repeated experience and explicit comparisons help students recognize that the smaller the length unit, the larger the number of units, and
 the larger the length unit, the smaller the number of units.

	Module 2	: Addition and Subtraction of Length Units
		Pacing:
	Se	eptember 30, 2019 ⁻ October 18, 2019
		Suggested Instructional Days = 14
Торіс	Lesson	Student Lesson Objective/ Supportive Videos
Topic A: Understand Con-	Lesson 1	Connect measurement with physical units by using multiple copies of the same physical unit to measure
cepts about the		https://www.youtube.com/watch?v Use iteration with one physical unit to measure.
Ruler	Lesson 2&3	Apply concepts to create unit rulers and measure lengths using unit rulers
		https://www.youtube.com/watch?v https://www.youtube.com/watch?v
Topic B: Measure and Es- timate Length Using Different Measurement Tools	Lesson 4 & 5	Measure various objects using centimeter rulers and meter sticks Develop estimation strategies by applying prior knowledge of length and using mental benchmarks <u>https://www.youtube.com/watch?v</u> <u>https://www.youtube.com/watch?v</u>
Topic C:	Lesson 6	Measure and compare lengths using centimeters and meters
Measure and		https://www.youtube.com/watch?v
Compare Lengths Using Different Length Units	Lesson 7	Measure and compare lengths using standard metric length units and non-standard length units; relate measurement to unit size https://www.youtube.com/watch?v
	Lesson 8	Solve addition and subtraction word problems using the ruler as a number line. https://www.youtube.com/watch?v
Topic D: Relate Addition and	Lesson 9	Measure lengths of string using measurement tools and use tape di- agrams to represent and compare the lengths. https://www.youtube.com/watch?v
Subtraction to Length	Lesson 10	Apply conceptual understanding of measurement by solving two- step word problems
		https://www.youtube.com/watch?v
		End-of- Module Assessment

Modifications						
Special Education/ 504:	English Language Learners:					
 -Adhere to all modifications and health concerns stated in each IEP. -Give students a Menu, allowing students to pick assignments from different levels based on difficulty. -Accommodate Instructional Strategies: reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), handouts, definition list with visuals, extended time -Allow students to demonstrate understanding of a problem by drawing the picture of the answer and then explaining the reasoning orally and/or in writing, such as Read-Draw-Write -Provide breaks between tasks, use positive reinforcement, use proximity -Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum by using manipulatives -Common Core Approach to Differentiate Instruction: Students with Disabilities (pg 17-18) -Strategies for Students with 504 Plans 	 Use manipulatives to promote conceptual understanding and enhance vocabulary usage Provide graphic representations, gestures, drawings, equations, realia, and pictures during all segments of instruction During i-Ready lessons, click on "Español" to hear specific words in Spanish Utilize graphic organizers which are concrete, pictorial ways of constructing knowledge and organizing information Use sentence frames and questioning strategies so that students will explain their thinking/ process of how to solve word problems Utilize program translations (if available) for L1/ L2 students Reword questions in simpler language Make use of the ELL Mathematical Language Routines (click here for additional information) Scaffolding instruction for ELL Learners Common Core Approach to Differentiate Instruction: Students with Disabilities (pg 16-17) 					
Gifted and Talented:	Students at Risk for Failure:					
 Elevated contextual complexity Inquiry based or open ended assignments and projects More time to study concepts with greater depth Promote the synthesis of concepts and making real world connections Provide students with enrichment practice that are imbedded in the curriculum such as: Application / Conceptual Development Are you ready for more? Common Core Approach to Differentiate Instruction: Students with Disabilities (pg. 20) Provide opportunities for math competitions Alternative instruction pathways available 	 Assure students have experiences that are on the Concrete- Pictorial- Abstract spectrum Modify Instructional Strategies, reading aloud text, graphic organizers, one-on-one instruction, class website (Google Classroom), inclusion of more visu- als and manipulatives, Field Trips, Google Expedi- tions, Peer Support, one on one instruction Assure constant parental/ guardian contact through- out the year with successes/ challenges Provide academic contracts to students and guardi- ans Create an interactive notebook with samples, key vocabulary words, student goals/ objectives. Always plan to address students at risk in your learning tasks, instructions, and directions. Try to an- ticipate where the needs will be and then address them prior to lessons. Common Core Approach to Differentiate Instruc- tion: Students with Disabilities (pg 19) 					

21st Century Life and Career Skills:

Career Ready Practices describe the career-ready skills that all educators in all content areas should seek to develop in their students. They are practices that have been linked to increase college, career, and life success. Career Ready Practices should be taught and reinforced in all career exploration and preparation programs with increasingly higher levels of complexity and expectation as a student advances through a program of

study.

https://www.state.nj.us/education/cccs/2014/career/9.pdf

 CRP1. Act as a responsible and contributing citizen and employee. CRP2. Apply appropriate academic and technical skills. CRP3. Attend to personal health and financial well-being. CRP4. Communicate clearly and effectively and with reason. CRP5. Consider the environmental, social and economic impacts of decisions. CRP6. Demonstrate creativity and innovation. 	 CRP7. Employ valid and reliable research strategies. CRP8. Utilize critical thinking to make sense of problems and persevere in solving them. CRP9. Model integrity, ethical leadership and effective management. CRP10. Plan education and career paths aligned to personal goals. CRP11. Use technology to enhance productivity. CRP12. Work productively in teams while using cultural global competence.
use of technical language. They are encourag	nicate with peers effectively, clearly, and with the ed to reason through experiences that promote crit- of perseverance. Students are exposed to various ng, calculators, and educational websites.

Technology Standards:

All students will be prepared to meet the challenge of a dynamic global society in which they participate, contribute, achieve, and flourish through universal access to people, information, and ideas. https://www.state.nj.us/education/cccs/2014/tech/

8.1 Educational Technology:

All students will use digital tools to access, manage, evaluate, and synthesize information in order to solve problems individually and collaborate and to create and communicate knowledge.

- A. **Technology Operations and Concepts:** Students demonstrate a sound understanding of technology concepts, systems and operations.
- B. Creativity and Innovation: Students demonstrate creative thinking, construct knowledge and develop innovative products and process using technology.
- C. Communication and Collaboration: Students use digital media and environments to communicate and work collaboratively, including at a distance, to support individual learning and contribute to the learning of others.
- D. **Digital Citizenship:** Students understand human, cultural, and societal issues related to technology and practice legal and ethical behavior.
- E. **Research and Information Fluency:** Students apply digital tools to gather, evaluate, and use of information.
- F. Critical thinking, problem solving, and decision making: Students use critical thinking skills to plan and conduct research, manage projects, solve problems, and make informed decisions using appropriate digital tools and resources.

8.2 Technology Education, Engineering, Design, and Computational Thinking -Programming:

All students will develop an understanding of the nature and impact of technology, engineering, technological design, computational thinking and the designed world as they relate to the individual, global society, and the environment.

- A. The Nature of Technology: Creativity and Innovation- Technology systems impact every aspect of the world in which we live.
- B. **Technology and Society:** Knowledge and understanding of human, cultural, and societal values are fundamental when designing technological systems and products in the global society.
- C. **Design:** The design process is a systematic approach to solving problems.
- D. Abilities in a Technological World: The designed world in a product of a design process that provides the means to convert resources into products and systems.
- E. **Computational Thinking: Programming-**Computational thinking builds and enhances problem solving, allowing students to move beyond using knowledge to creating knowledge.

Interdisciplinary Connections:				
English Lar	nguage Arts:			
RF.2.4	Read with sufficient accuracy and fluency to support comprehension.			
SL.2.1	Participate in collaborative conversations with diverse partners about <i>grade 2 topics and texts</i> with peers and adults in small and larger groups.			
L.2.4	Determine or clarify the meaning of unknown and multiple-meaning words and phrases based on grade 2 reading and content, choosing flexibly from an array of strategies.			

NJSLS Unpacked Standards

2.MD.1

Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.

Second Graders build upon their non-standard measurement experiences in First Grade by measuring in standard units for the first time. Using both customary (inches and feet) and metric (centimeters and meters) units, Second Graders select an attribute to be measured (e.g., length of classroom), choose an appropriate unit of measurement (e.g., yardstick), and determine the number of units (e.g., yards). As teachers provide rich tasks that ask students to perform real measurements, these foundational understandings of measurement are developed:

- Understand that larger units (e.g., yard) can be subdivided into equivalent units (e.g., inches) (partition).
- Understand that the same object or many objects of the same size such as paper clips can be repeatedly used to determine the length of an object (iteration).
- Understand the relationship between the size of a unit and the number of units needed (compensatory principal). Thus, the smaller the unit, the more units it will take to measure the selected attribute.

When Second Grade students are provided with opportunities to create and use a variety of rulers, they can connect their understanding of non-standard units from First Grade to standard units in second grade. For example:

By helping students progress from a "ruler" that is blocked off into colored units (no numbers)	
to a "ruler" that has numbers along with the colored units	1 2 3 4 5 6 7 8
to a "ruler" that has inches (centimeters) with and without numbers, students develop the understanding that the numbers on a ruler do not count the individual marks but indicate the spaces (distance) between the marks. This is a critical under-	
stand students need when using such tools as rulers, yardsticks, meter sticks, and measuring tapes.	

By the end of Second Grade, students will have also learned specific measurements as it relates to feet, yards and meters:

- There are 12 inches in a foot.
- There are 3 feet in a yard.

There are 100 centimeters in a meter

2.MD.2

Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen

Second Grade students measure an object using two units of different lengths. This experience helps students realize that the unit used is as important as the attribute being measured. This is a difficult concept for young children and will require numerous experiences for students to predict, measure, and discuss outcomes.

Example: A student measured the length of a desk in both feet and inches. She found that the desk was 3 feet long. She also found out that it was 36 inches long.

Teacher: Why do you think you have two different measurements for the same desk? **Student**: It only took 3 feet because the feet are so big. It took 36 inches because an inch is a whole lot smaller than a foot.

2.MD.3

Estimate lengths using units of inches, feet, centimeters, and meters

Second Grade students estimate the lengths of objects using inches, feet, centimeters, and meters prior to measuring. Estimation helps the students focus on the attribute being measured and the measuring process. As students estimate, the student has to consider the size of the unit- helping them to become more familiar with the unit size. In addition, estimation also creates a problem to be solved rather than a task to be completed. Once a student has made an estimate, the student then measures the object and reflects on the accuracy of the estimate made and considers this information for the next measurement.

Example:

Teacher: How many inches do you think this string is if you measured it with a ruler?

Student: An inch is pretty small. I'm thinking it will be somewhere between 8 and 9 inches.

Teacher: Measure it and see.

Student: It is 9 inches. I thought that it would be somewhere around there.

2.MD.4

Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit

Second Grade students determine the difference in length between two objects by using the same tool and unit to measure both objects. Students choose two objects to measure, identify an appropriate tool and unit, measure both objects, and then determine the differences in lengths.

Example:

Teacher: Choose two pieces of string to measure. How many inches do you think each string is?

Student: I think String A is about 8 inches long. I think string B is only about 4 inches long. It's really short. **Teacher**: Measure to see how long each string is. *Student measures*. What did you notice?

Student: String A is definitely the longest one. It is 10 inches long. String B was only 5 inches long. I was close! **Teacher**: How many more inches does your short string need to be so that it is the same length as your long string? **Student**: Hmmm. String B is 5 inches. It would need 5 more inches to be 10 inches. 5 and 5 is 10



Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

Second Grade students apply the concept of length to solve addition and subtraction word problems with numbers within 100. Students should use the same unit of measurement in these problems. Equations may vary depending on students' interpretation of the task. Notice in the examples below that these equations are similar to those problem types in Table 1 at the end of this document.

Example: In P.E. class Kate jumped 14 inches. Mary jumped 23 inches. How much farther did Mary jump than Kate? Write an equation and then solve the problem.

Student A

My equation is $14 + _ = 23$ since I thought, "14 and what makes 23?". I used Unifix cubes. I made a train of 14. Then I made a train of 23. When I put them side by side, I saw that Kate would need 9 more cubes to be the same as Mary. So, Mary jumped 9 more inches than Kate. 14 + 9 = 23.

 Student B My equation is 23 - 14 = ____ since I thought about what the difference was between Kate and Mary. I broke up 14 into 10 and 4. I know that 23 minus 10 is 13. Then, I broke up the 4 into 3 and 1. 13 minus 3 is 10. Then, I took one more away. That left me with 9. So, Mary jumped 9 more inches than Kate. That seems to make sense since 23 is almost 10 more than 14. 23 - 14 = 9.

> 23 - 10 = 1313 - 3 = 1010 - 1 = 9

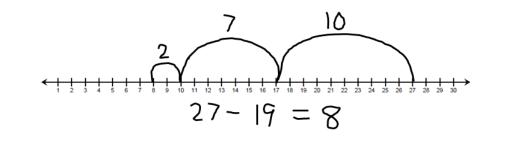
	Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corre-
2.MD.6	sponding to the numbers 0, 1, 2,, and represent whole-number sums and differences within 100 on a
	number line diagram.

Building upon their experiences with open number lines, Second Grade students create number lines with evenly spaced points corresponding to the numbers to solve addition and subtraction problems to 100. They recognize the similarities between a number line and a ruler.

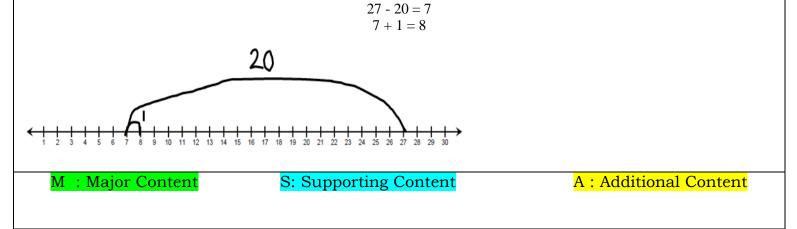
•	<u> </u>	-	+	+	-	+	+	-	+	+	•
				•	•						-

Example: There were 27 students on the bus. 19 got off the bus. How many students are on the bus?

Student A: I used a number line. I started at 27. I broke up 19 into 10 and 9. That way, I could take a jump of 10. I landed on 17. Then I broke the 9 up into 7 and 2. I took a jump of 7. That got me to 10. Then I took a jump of 2. That's 8. So, there are 8 students now on the bus.



Student B: I used a number line. I saw that 19 is really close to 20. Since 20 is a lot easier to work with, I took a jump of 20. But, that was one too many. So, I took a jump of 1 to make up for the extra. I landed on 8. So, there are 8 students on the bus.



Common addition and subtraction.¹

	RESULT UNKNOWN	CHANGE UNKNOWN	START UNKNOWN
	Two bunnies sat on the grass.	Two bunnies were sitting on	Some bunnies were sitting on
	Three more bunnies hopped	the grass. Some more bunnies	the grass. Three more bunnies
ADD TO	there. How many bunnies are	hopped there. Then there were	hopped there. Then there wer
ADD TO	on the grass now? 2+3=?	five bunnies. How many	five bunnies. How many
		bunnies hopped over to the	bunnies were on the grass
		first two? 2 + ? = 5	before??+3=5
	Five apples were on the table. I	Five apples were on the table. I	Some apples were on the table
	ate two apples. How many	ate some apples. Then there	I ate two apples. Then there
TAKE FROM	apples are on the table now?5-	were three apples. How many	were three apples. How many
	2=?	apples did I eat?5 - ? = 3	apples were on the table
			before??-2 = 3
	TOTAL UNKNOWN	ADDEND UNKNOWN	BOTH ADDENDS
			UNKNOWN ²
	Three red apples and two green	Five apples are on the table.	Grandma has five flowers. Ho
	apples are on the table. How	Three are red and the rest are	many can she put in the red
PUT TOGETHER / TAKE APART ³	many apples are on the table? 3	green. How many apples are	vase and how many in her blu
IAKE APART -	+ 2 = ?	green? 3+?=5,5-3=?	vase? 5 = 0 + 5, 5 + 0 5 = 1 + 4
			= 4+1, 5 = 2 + 3, 5 = 3 + 2
			-4+1,5-2+3,5-3+2
COMPARE	DIFFERENCE UKNOWN	BIGGER UNKNOWN	SMALLER UNKNOWN
COMPARE	DIFFERENCE UKNOWN ("How many more?"	BIGGER UNKNOWN (Version with "more"): Julie has	SMALLER UNKNOWN
COMPARE			SMALLER UNKNOWN (Version with "more"): Julie ha
COMPARE	("How many more?"	(Version with "more"): Julie has	SMALLER UNKNOWN (Version with "more"): Julie ha three more apples than Lucy.
COMPARE	("How many more?" version):Lucy has two apples.	(Version with "more"): Julie has three more apples than	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How mar
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How	SMALLER UNKNOWN (Version with "more"):Julie ha three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Versio
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have?	SMALLER UNKNOWN (Version with "more"): Julie ha
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?"	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has	SMALLER UNKNOWN (Version with "more"):Julie has three more apples than Lucy. Julie has five apples. How mar apples does Lucy have?(Versio with "fewer"): Lucy has 3 fewe apples than Julie. Julie has five
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?" version): Lucy has two apples. Julie has five apples. How many fewer apples does Lucy have	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has 3 fewer apples than Julie. Lucy	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Versio with "fewer"): Lucy has 3 fewe
COMPARE	("How many more?" version):Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?("How many fewer?" version): Lucy has two apples. Julie has five apples. How many	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have? (Version with "fewer"): Lucy has 3 fewer apples than Julie. Lucy has two apples. How many	SMALLER UNKNOWN (Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How man apples does Lucy have?(Versio with "fewer"): Lucy has 3 fewe apples than Julie. Julie has five apples. How many apples doe

¹ Adapted from Box 2-4 of Mathematics Learning in Early Childhood, National Research Council (2009, pp. 32, 33).

² These take apart situations can be used to show all the decompositions of a given number. The associated equations, which have the total on the left of the equal sign, help children understand that the – sign does not always mean, makes or results in but always does mean is the same number as.

³ Either addend can be unknown, so there are three variations of these problem situations. Both addends Unknown is a productive extension of the basic situation, especially for small numbers less than or equal to 10.

⁴ For the Bigger Unknown or Smaller Unknown situations, one version directs the correct operation (the version using more for the bigger unknown and using less for the smaller unknown). The other versions are more difficult.

http://www.corestandards.org/Math/Content/mathematics-glossary/Table-1/

Module 2 Assessment Framework			
Assessment	NJSLS	Estimated Time	Format
Optional End-of- Module			Individual or
Assessment	2.MD.1-6	1 Block	Small Group with
(Interview Style)			Teacher

Module 2 Performance Assessment/ PBL Framework				
Assessment	NJSLS	Estimated Time	Format	
Module 2 Performance Task 1 High Jump Competition	2.MD.5	Up to 30 minutes	Individual or Small Group	
Extended Constructed Response (ECR)* (click here for access)	Dependent on unit of study & month of administration	Up to 30 Minutes	Individual	

Use the following links to access ECR protocol and district assessment scoring documents:

- Assessment and Data in Mathematics Bulletin
- ECR Protocol

Second Grade Ideal Math Block

Fluency: Whole Group

Sprints, Counting, Whiteboard Exchange

Application Problem: Whole Group

Provides HANDS-ON work to allow children to ACT OUT or ENGAGE ACTIVELY with the new MATH IDEA Technology Integration: https://embarc.online/

*Website provides Goggle slides, additional activities, and student videos per lesson

Concept Development: Individual/partner/whole

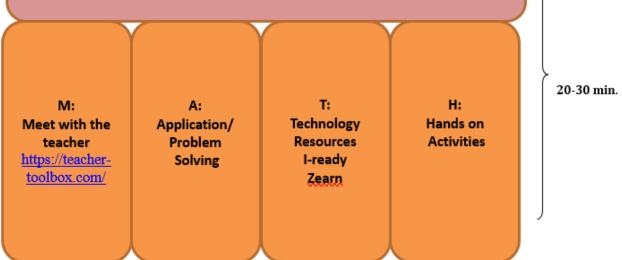
Instruction & Strategic Problem Set Questions Technology Integration: <u>https://embarc.online/</u> Website provides Goggle slides, additional activities, and student videos. per lesson

Student Debrief: Whole Group

Exit Ticket: Independent

CENTERS/STATIONS: Pairs / Small Group/ Individual

DIFFERENTIATED activities designed to RETEACH, REMEDIATE, ENRICH student's understanding of concepts.



50-60 min

Lesson Structure:

Fluency:

- Sprints
- Whiteboard Exchange

Technology Integration:

Splat Sequences

Which one doesn't belong?

Would you rather?

Esti- Mysteries

Anchor Task:

- Engage students in using the RDW Process
- Sequence problems from simple to complex and adjust based on students' responses
- Facilitate share and critique of various explanations, representations, and/or examples.

Guided Practice/ Independent Practice : (largest chunk of time)

Instruction:

- Maintain overall alignment with the objectives and suggested pacing and structure.
- Use of tools, precise mathematical language, and/or models
- Balance teacher talk with opportunities for peer share and/or collaboration
- Generate next steps by watching and listening for understanding

Problem Set: (Individual, partner, or group)

- Allow for independent practice and productive struggle
- Assign problems strategically to differentiate practice as needed
- Create and assign remedial sequences as needed

Technology Integration:

- Think Central:
 - Pre-Test
 - Chapter Review
 - Test Prep
 - Performance Tasks

https://embarc.online/

Virtual Manipulatives for lessons

http://nlvm.usu.edu/en/nav/vlibrary.html

For videos that students can watch and interact with independently click here

Student Debrief:

- Elicit students thinking, prompt reflection, and promote metacognition through student centered discussion
- Culminate with students' verbal articulation of their learning for the day
- Close with completion of the daily Exit Ticket (opportunity for informal assessment that guides effective preparation of subsequent lessons) as needed.

Centers:

- I-Ready: <u>https://login.i-ready.com/</u> *i-Ready* makes the promise of differentiated instruction a practical reality for teachers and students. It was designed to get students excited about learning and to support teachers in the challenge of meeting the needs of all learners. Through the power of one intuitive system whose pieces were built from the ground up to work together, teachers have the tools they need to ensure students are on the road to proficiency.
- Zearn: <u>https://www.zearn.org/</u>Zearn Math is a K-5 math curriculum based on Eureka Math with top-rated materials for teacher-led and digital instruction.
- Teacher Toolbox; <u>https://teacher-toolbox.com/</u> A digital collection of K-8 resources to help you differentiate instruction to students performing on, below, and above grade level.

NJSLS	Evidence Statement	Clarification	Math Practices
2.MD.1	Measure the length of an object by se- lecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes	 i)Length may be measured in whole units within the same measurement system using metric or U.S. customary. ii) Units are limited to those found in 2.MD.3 	MP 5
2.MD.2	Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen.	 i)Tasks should be limited to whole units with- in the same measurement system. ii) Units are limited to those found in 2.MD.3 iii) Example: Student measures the length of a table in inches and in feet and notes that the number of feet is less than the number of inches because an inch is smaller than a foot. Therefore, it takes more inch units than foot units to measure the table's length 	MP 5
2.MD.3	Estimate lengths using units of inches, feet, centimeters, and meters.	i) Rulers are not used to estimate.	MP 5,6
2.MD.4	Measure to determine how much longer one object is than another, expressing the length difference in terms of a stand- ard length unit.	i.Length may be measured in whole units within the same measurement system using metric or U.S. customary. ii. Units are limited to those in 2.MD.3.	MP 5,6

Number Talks

What does Number Talks look like?

- Students are near each other so they can communicate with each other (central meeting place)
- Students are mentally solving problems
- Students are given thinking time
- Thumbs up show when they are ready
- Teacher is recording students' thinking

Communication

- Having to talk out loud about a problem helps students clarify their own thinking
- Allow students to listen to other's strategies and value other's thinking
- Gives the teacher the opportunity to hear student's thinking

Mental Math

- When you are solving a problem mentally you must rely on what you know and understand about the numbers instead of memorized procedures
- You must be efficient when computing mentally because you can hold a lot of quantities in your head

Thumbs Up

- This is just a signal to let you know that you have given your students enough time to think about the problem
- If will give you a picture of who is able to compute mentally and who is struggling
- It isn't as distracting as a waving hand

Teacher as Recorder

- Allows you to record students' thinking in the correct notation
- Provides a visual to look at and refer back to
- Allows you to keep a record of the problems posed and which students offered specific strategies

Purposeful Problems

- Start with small numbers so the students can learn to focus on the strategies instead of getting lost in the numbers
- Use a number string (a string of problems that are related to and scaffold each other)

Starting Number Talks in your Classroom

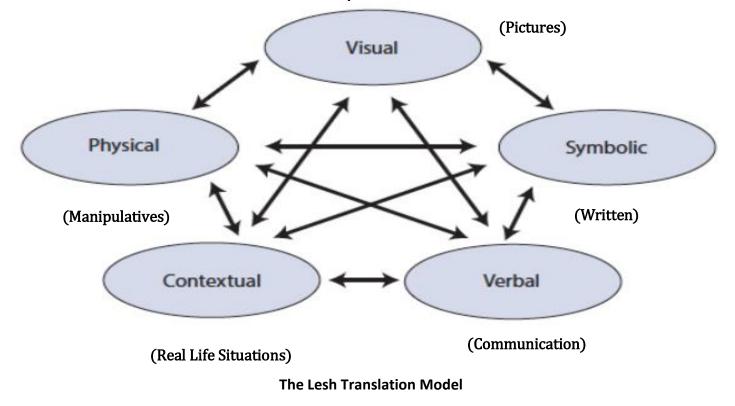
- Start with specific problems in mind
- Be prepared to offer a strategy from a previous student
- It is ok to put a student's strategy on the backburner
- Limit your number talks to about 15 minutes
- Ask a question, don't tell!

The teacher asks questions:

- Who would like to share their thinking?
- Who did it another way?
- How many people solved it the same way as Billy?
- Does anyone have any questions for Billy?
- Billy, can you tell us where you got that 5?
- How did you figure that out?

Second Grade Unit 2: Add/ Subtract Length

Student Name: Date:	Task: School: Teacher:				
	STUDENT FRIENDLY RUBRIC			SCORE	
"I CAN"	a start 1	getting there 2	that's it 3	WOW! 4	SCORE
Understand	l need help.	I need some help.	l do not need help.	I can help a class- mate.	
Solve	I am unable to use a strategy.	l can start to use a strategy.	l can solve it more than one way.	I can use more than one strategy and talk about how they get to the same answer.	
Say or Write	I am unable to say or write.	l can write or say some of what I did.	I can write and talk about what I did. I can write or talk about why I did it.	I can write and say what I did and why I did it.	
Draw or Show	I am not able to draw or show my thinking.	I can draw, but not show my thinking; or I can show but not draw my thinking;	I can draw and show my thinking	I can draw, show and talk about my think- ing.	



Use and Connection of Mathematical Representations

Each oval in the model corresponds to one way to represent a mathematical idea.

Visual: When children draw pictures, the teacher can learn more about what they understand about a particular mathematical idea and can use the different pictures that children create to provoke a discussion about mathematical ideas. Constructing their own pictures can be a powerful learning experience for children because they must consider several aspects of mathematical ideas that are often assumed when pictures are pre-drawn for students.

Physical: The manipulatives representation refers to the unifix cubes, base-ten blocks, fraction circles, and the like, that a child might use to solve a problem. Because children can physically manipulate these objects, when used appropriately, they provide opportunities to compare relative sizes of objects, to identify patterns, as well as to put together representations of numbers in multiple ways.

Second Grade Unit 2: Add/ Subtract Length

Verbal: Traditionally, teachers often used the spoken language of mathematics but rarely gave students opportunities to grapple with it. Yet, when students do have opportunities to express their mathematical reasoning aloud, they may be able to make explicit some knowledge that was previously implicit for them.

Symbolic: Written symbols refer to both the mathematical symbols and the written words that are associated with them. For students, written symbols tend to be more abstract than the other representations. I tend to introduce symbols after students have had opportunities to make connections among the other representations, so that the students have multiple ways to connect the symbols to mathematical ideas, thus increasing the likelihood that the symbols will be comprehensible to students.

Contextual: A relevant situation can be any context that involves appropriate mathematical ideas and holds interest for children; it is often, but not necessarily, connected to a real-life situation.

The Lesh Translation Model: Importance of Connections

As important as the ovals are in this model, another feature of the model is even more important than the representations themselves: The arrows! The arrows are important because they represent the connections students make between the representations. When students make these connections, they may be better able to access information about a mathematical idea, because they have multiple ways to represent it and, thus, many points of access.

Individuals enhance or modify their knowledge by building on what they already know, so the greater the number of representations with which students have opportunities to engage, the more likely the teacher is to tap into a student's prior knowledge. This "tapping in" can then be used to connect students' experiences to those representations that are more abstract in nature (such as written symbols). Not all students have the same set of prior experiences and knowledge. Teachers can introduce multiple representations in a meaning-ful way so that students' opportunities to grapple with mathematical ideas are greater than if their teachers used only one or two representations.

Concrete Pictorial Abstract (CPA) Instructional Approach

The CPA approach suggests that there are three steps necessary for pupils to develop understanding of a mathematical concept.

Concrete: "Doing Stage": Physical manipulation of objects to solve math problems.Pictorial: "Seeing Stage": Use of imaged to represent objects when solving math problems.Abstract: "Symbolic Stage": Use of only numbers and symbols to solve math problems.

CPA is a gradual systematic approach. Each stage builds on to the previous stage. Reinforcement of concepts are achieved by going back and forth between these representations and making connections between stages. Students will benefit from seeing parallel samples of each stage and how they transition from one to another.

Read, Draw, Write Process

READ the problem. Read it over and over.... And then read it again.

DRAW a picture that represents the information given. During this step students ask themselves: Can I draw something from this information? What can I draw? What is the best model to show the information? What conclusions can I make from the drawing?

WRITE your conclusions based on the drawings. This can be in the form of a number sentence, an equation, or a statement.

Students are able to draw a model of what they are reading to help them understand the problem. Drawing a model helps students see which operation or operations are needed, what patterns might arise, and which models work and do not work. Students must dive deeper into the problem by drawing models and determining which models are appropriate for the situation.

While students are employing the RDW process they are using several Standards for Mathematical Practice and in some cases, all of them.

Mathematical Discourse and Strategic Questioning

Discourse involves asking strategic questions that elicit from students their understanding of the context and actions taking place in a problem, how a problem is solved and why a particular method was chosen. Students learn to critique their own and others' ideas and seek out efficient mathematical solutions.

While classroom discussions are nothing new, the theory behind classroom discourse stems from constructivist views of learning where knowledge is created internally through interaction with the environment. It also fits in with sociocultural views on learning where students working together are able to reach new understandings that could not be achieved if they were working alone.

Underlying the use of discourse in the mathematics classroom is the idea that mathematics is primarily about reasoning not memorization. Mathematics is not about remembering and applying a set of procedures but about developing understanding and explaining the processes used to arrive at solutions.

Teacher Questioning:

Asking better questions can open new doors for students, promoting mathematical thinking and classroom discourse. Can the questions you're asking in the mathematics classroom be answered with a simple "yes" or "no," or do they invite students to deepen their understanding?



Albert Einstein

To help you encourage deeper discussions, here are 100 questions to incorporate into your instruction by

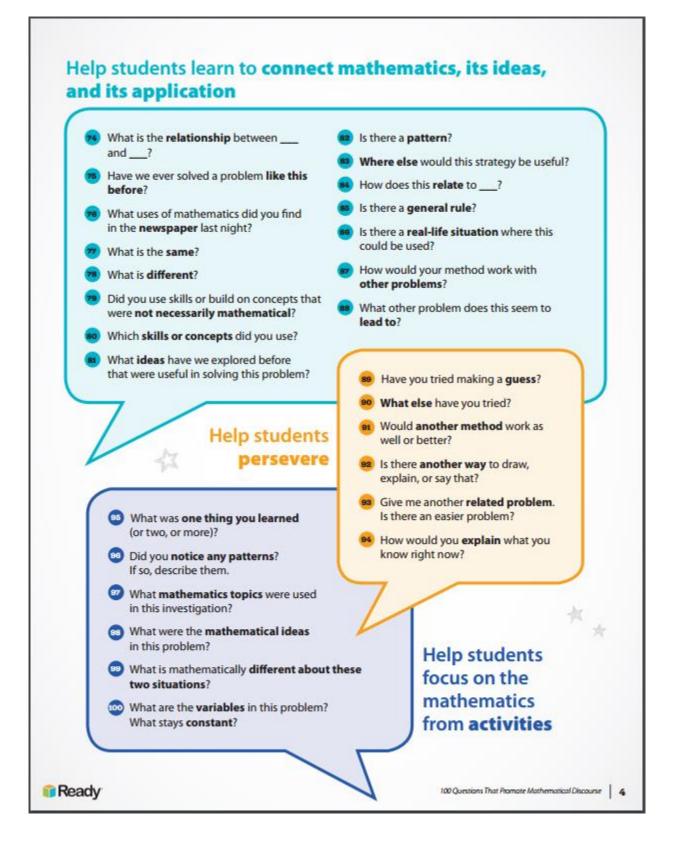
Gladis Kersaint, mathematics expert and advisor for Ready Mathematics.

Disco	ematical
 What strategy did you use? Do you agree? Do you disagree? Would you ask the rest of the class that question? Could you share your method with the class? What part of what he said do you understand? Would someone like to share? Can you convince the rest of us the your answer makes sense? What do others think about what [student] said? 	 Have you discussed this with your group? With others? Did anyone get a different answer? Where would you go for help? Did everybody get a fair chance to talk, use the manipulatives, or be the recorder? How could you help another student without telling them the answer?
Help students rely more on themselves to determine whether something is mathematically correct	 Is this a reasonable answer? Does that make sense? Why do you think that? Why is that true? Can you draw a picture or make a model to show that? How did you reach that conclusion? Does anyone want to revise his or her answer? How were you sure your answer was right?

Dr.







Conceptual Understanding

Students demonstrate conceptual understanding in mathematics when they provide evidence that they can:

- recognize, label, and generate examples of concepts;
- use and interrelate models, diagrams, manipulatives, and varied representations of concepts;
- identify and apply principles; know and apply facts and definitions;
- compare, contrast, and integrate related concepts and principles; and
- recognize, interpret, and apply the signs, symbols, and terms used to represent concepts.

Conceptual understanding reflects a student's ability to reason in settings involving the careful application of concept definitions, relations, or representations of either.

Procedural Fluency

Procedural fluency is the ability to:

- apply procedures accurately, efficiently, and flexibly;
- to transfer procedures to different problems and contexts;
- to build or modify procedures from other procedures; and
- to recognize when one strategy or procedure is more appropriate to apply than another.

Procedural fluency is more than memorizing facts or procedures, and it is more than understanding and being able to use one procedure for a given situation. Procedural fluency builds on a foundation of conceptual understanding, strategic reasoning, and problem solving (NGA Center & CCSSO, 2010; NCTM, 2000, 2014). Research suggests that once students have memorized and practiced procedures that they do not understand, they have less motivation to understand their meaning or the reasoning behind them (Hiebert, 1999). Therefore, the development of students' conceptual understanding of procedures should precede and coincide with instruction on procedures.

Math Fact Fluency: Automaticity

Students who possess math fact fluency can recall math facts with automaticity. Automaticity is the ability to do things without occupying the <u>mind</u> with the low-level details required, allowing it to become an automatic response pattern or <u>habit</u>. It is usually the result of <u>learning</u>, <u>repetition</u>, and practice.

K-2 Math Fact Fluency Expectation

K.OA.5 Add and Subtract within 5.1.OA.6 Add and Subtract within 10.2.OA.2 Add and Subtract within 20.

Math Fact Fluency: Fluent Use of Mathematical Strategies

First and second grade students are expected to solve addition and subtraction facts using a variety of strategies fluently.

1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as:

- counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14);
- decomposing a number leading to a ten (e.g., 13 4 = 13 3 1 = 10 1 = 9);
- using the relationship between addition and subtraction; and
- creating equivalent but easier or known sums.

2.NBT.7 Add and subtract within 1000, using concrete models or drawings and strategies based on:

- o place value,
- o properties of operations, and/or
- o the relationship between addition and subtraction;

Evidence of Student Thinking

Effective classroom instruction and more importantly, improving student performance, can be accomplished when educators know how to elicit evidence of students' understanding on a daily basis. Informal and formal methods of collecting evidence of student understanding enable educators to make positive instructional changes. An educators' ability to understand the processes that students use helps them to adapt instruction allowing for student exposure to a multitude of instructional approaches, resulting in higher achievement. By highlighting student thinking and misconceptions, and eliciting information from more students, all teachers can collect more representative evidence and can therefore better plan instruction based on the current understanding of the entire class.

Mathematical Proficiency

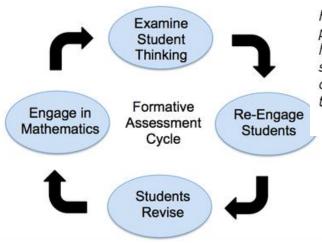
To be mathematically proficient, a student must have:

- <u>Conceptual understanding</u>: comprehension of mathematical concepts, operations, and relations;
- <u>Procedural fluency</u>: skill in carrying out procedures flexibly, accurately, efficiently, and appropriately;
- <u>Strategic competence</u>: ability to formulate, represent, and solve mathematical problems;
- <u>Adaptive reasoning</u>: capacity for logical thought, reflection, explanation, and justification;
- Productive disposition: habitual inclination to see mathematics as sensible, useful, and worthwhile,

coupled with a belief in diligence and one's own efficacy.

Evidence should:

- Provide a window in student thinking;
- Help teachers to determine the extent to which students are reaching the math learning goals; and
- Be used to make instructional decisions during the lesson and to prepare for subsequent lessons.



Formative assessment is an essentially interactive process, in which the teacher can find out whether what has been taught has been learned, and if not, to do something about it. Day-to-day formative assessment is one of the most powerful ways of improving learning in the mathematics classroom.

(Wiliam 2007, pp. 1054; 1091)

Connections to the Mathematical Practices

Student Friendly Connections to the Mathematical Practices

- 1. I can solve problems without giving up.
- 2. I can think about numbers in many ways.
- 3. I can explain my thinking and try to understand others.
- 4. I can show my work in many ways.
- 5. I can use math tools and tell why I choose them.
- 6. I can work carefully and check my work.
- 7. I can use what I know to solve new problems.
- 8. I can discover and use short cuts.

The **Standards for Mathematical Practice** describe varieties of expertise that mathematics educators at all levels should seek to develop in their students.

Make sense of problems and persevere in solving them

In Kindergarten, students learn that doing math involves solving problems and discussing how they solved them. Students will begin to explain the meaning of a problem, and look for ways to solve it. Kindergarteners will learn how to use objects and pictures to help them understand and solve problems. They will begin to check their thinking when the teacher asks them how they got their answer, and if the answer makes sense. When working in small groups or with a partner they will listen to the strategies of the group and will try different approaches.

Reason abstractly and quantitatively

1

2

Mathematically proficient students in Kindergarten make sense of quantities and the relationships while solving tasks. This involves two processes- decontextualizing and contextualizing. In Kindergarten, students represent situations by decontextualizing tasks into numbers and symbols. For example, in the task, "There are 7 children on the playground and some children go line up. If there are 4 children still playing, how many children lined up?" Kindergarten students are expected to translate that situation into the equation: 7-4 =____, and then solve the task. Students also contextualize situations during the problem solving process. For example, while solving the task above, students refer to the context of the task to determine that they need to subtract 4 since the number of children on the playground is the total number of students except for the 4 that are still playing. Abstract reasoning also occurs when students measure and compare the lengths of objects.

Construct viable arguments and critique the reasoning of others

Mathematically proficient students in Kindergarten accurately use mathematical terms to construct arguments and engage in discussions about problem solving strategies. For example, while solving the task, "There are 8 books on the shelf. If you take some books off the shelf and there are now 3 left, how many books did you take off the shelf?"

3 the shelf. If you take some books off the shelf and there are now 3 left, how many books did you take off the shelf?' students will solve the task, and then be able to construct an accurate argument about why they subtracted 3 form 8 rather than adding 8 and 3. Further, Kindergarten students are expected to examine a variety of problem solving strategies and begin to recognize the reasonableness of them, as well as similarities and differences among them.

Model with mathematics

4

5

Mathematically proficient students in Kindergarten model real-life mathematical situations with a number sentence or an equation, and check to make sure that their equation accurately matches the problem context. Kindergarten students rely on concrete manipulatives and pictorial representations while solving tasks, but the expectation is that they will also write an equation to model problem situations. For example, while solving the task "there are 7 bananas on the counter. If you eat 3 bananas, how many are left?" Kindergarten students are expected to write the equation 7-3 = 4. Likewise, Kindergarten students are expected to create an appropriate problem situation from an equation. For example, students are expected to orally tell a story problem for the equation 4+5 = 9.

Use appropriate tools strategically

Mathematically proficient students in Kindergarten have access to and use tools appropriately. These tools may include counters, place value (base ten) blocks, hundreds number boards, number lines, and concrete geometric shapes (e.g., pattern blocks, 3-d solids). Students should also have experiences with educational technologies, such as calculators, virtual manipulatives, and mathematical games that support conceptual understanding. During classroom instruction, students should have access to various mathematical tools as well as paper, and determine which tools are the most appropriate to use. For example, while solving the task "There are 4 dogs in the park. If 3 more dogs show up, how many dogs are they?" Kindergarten students are expected to explain why they used specific mathematical tools."

Attend to precision

Mathematically proficient students in Kindergarten are precise in their communication, calculations, and measurements. In all mathematical tasks, students in Kindergarten describe their actions and strategies clearly, using gradelevel appropriate vocabulary accurately as well as giving precise explanations and reasoning regarding their process of finding solutions. For example, while measuring objects iteratively (repetitively), students check to make sure that there are no gaps or overlaps. During tasks involving number sense, students check their work to ensure the accuracy and reasonableness of solutions.

6

Look for and make use of structure

7

Mathematically proficient students in Kindergarten carefully look for patterns and structures in the number system and other areas of mathematics. While solving addition problems, students begin to recognize the commutative property, in that 1+4 = 5, and 4+1 = 5. While decomposing teen numbers, students realize that every number between 11 and 19, can be decomposed into 10 and some leftovers, such as 12 = 10+2, 13 = 10+3, etc. Further, Kindergarten students make use of structures of mathematical tasks when they begin to work with subtraction as missing addend problems, such as 5-1 =___ can be written as 1+__ = 5 and can be thought of as how much more do I need to add to 1 to get to 5?

Look for and express regularity in repeated reasoning

Mathematically proficient students in Kindergarten begin to look for regularity in problem structures when solving mathematical tasks. Likewise, students begin composing and decomposing numbers in different ways. For example, in the task "There are 8 crayons in the box. Some are red and some are blue. How many of each could there be?" Kindergarten students are expected to realize that the 8 crayons could include 4 of each color (4+4 = 8), 5 of one color and 3 of another (5+3 = 8), etc. For each solution, students repeated engage in the process of finding two numbers that can be joined to equal 8.

Effective Mathematics Teaching Practices

Establish mathematics goals to focus learning. Effective teaching of mathematics establishes clear goals for the mathematics that students are learning, situates goals within learning progressions, and uses the goals to guide instructional decisions.

Implement tasks that promote reasoning and problem solving. Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving and allow multiple entry points and varied solution strategies.

Use and connect mathematical representations. Effective teaching of mathematics engages students in making connections among mathematical representations to deepen understanding of mathematics concepts and procedures and as tools for problem solving.

Facilitate meaningful mathematical discourse. Effective teaching of mathematics facilitates discourse among students to build shared understanding of mathematical ideas by analyzing and comparing student approaches and arguments.

Pose purposeful questions. Effective teaching of mathematics uses purposeful questions to assess and advance students' reasoning and sense making about important mathematical ideas and relationships.

Build procedural fluency from conceptual understanding. Effective teaching of mathematics builds fluency with procedures on a foundation of conceptual understanding so that students, over time, become skillful in using procedures flexibly as they solve contextual and mathematical problems.

Support productive struggle in learning mathematics. Effective teaching of mathematics consistently provides students, individually and collectively, with opportunities and supports to engage in productive struggle as they grapple with mathematical ideas and relationships.

Elicit and use evidence of student thinking. Effective teaching of mathematics uses evidence of student thinking to assess progress toward mathematical understanding and to adjust instruction continually in ways that support and extend learning.

	5 Practices for Orchestrating Productive Mathematics Discussions
Practice	Description/ Questions
1. Anticipating	What strategies are students likely to use to approach or solve a challenging high-level mathematical task?
	How do you respond to the work that students are likely to produce?
	Which strategies from student work will be most useful in addressing the mathematical goals?
2. Monitoring	Paying attention to what and how students are thinking during the lesson.
	Students working in pairs or groups
	Listening to and making note of what students are discussing and the strategies they are using
	Asking students questions that will help them stay on track or help them think more deeply about the task. (Pr mote productive struggle)
3. Selecting	This is the process of deciding the <i>what</i> and the <i>who</i> to focus on during the discussion.
4. Sequencing	What order will the solutions be shared with the class?
5. Connecting	Asking the questions that will make the mathematics explicit and understandable.
	Focus must be on mathematical meaning and relationships; making links between mathematical ideas and rep sentations.

MATH CENTERS/ WORKSTATIONS

Math workstations allow students to engage in authentic and meaningful hands-on learning. They often last for several weeks, giving students time to reinforce or extend their prior instruction. Before students have an opportunity to use the materials in a station, introduce them to the whole class, several times. Once they have an understanding of the concept, the materials are then added to the work stations.

Station Organization and Management Sample

Teacher A has 12 containers labeled 1 to 12. The numbers correspond to the numbers on the rotation chart. She pairs students who can work well together, who have similar skills, and who need more practice on the same concepts or skills. Each day during math work stations, students use the center chart to see which box they will be using and who their partner will be. Everything they need for their station will be in their box. **Each station is differentiated**. If students need more practice and experience working on numbers 0 to 10, those will be the only numbers in their box. If they are ready to move on into the teens, then she will place higher number activities into the box for them to work with.



In the beginning there is a lot of prepping involved in gathering, creating, and organizing the work stations. However, once all of the initial work is complete, the stations are easy to manage. Many of her stations stay in rotation for three or four weeks to give students ample opportunity to master the skills and concepts.

Read *Math Work Stations* by Debbie Diller.

In her book, she leads you step-by-step through the process of implementing work stations.

MATH WORKSTATION INFORMATION CARD

Iath Workstation:	 Time:
SLS.:	
jective(s): By the end of this task, I will be able to:	
•	
•	
•	
•	
•	
•	
•	
kit Ticket:	
•	
•	
•	

Μ	ATH WORKSTATION	SCHEDULE		Week of:	
DAY	Technology Lab	Problem Solving Lab	Fluency Lab	Math Journal	Small Group In- struction
Mon.					
Tues	Group	Group	Group	Group	BASED
Tues.	Group	Group	Group	Group	ON CURRENT OB- SERVATIONAL DA-
Wed.	Group	Group	Group	Group	ТА
Thurs.	I	·	·		
	Group	Group	Group	Group	
Fri.					
	Group	Group	Group	Group	

INSTRUCTIONAL GROUPING

	GROUP A		GROUP B
1		1	
2		2	
3		3	
4		4	
5		5	
6		6	
	GROUP C		GROUP D
1		1	
2		2	
3		3	
4		4	
5		5	

Second Grade PLD Rubric

Go	t It		Not There Yet		
Evidence shows that the student essentially has the target concept		Student shows evidence of a major misunderstanding, incorrect concepts or procedure, or a failure to			
or big math idea.		engage in the task.			
PLD Level 5: 100%	PLD Level 4: 89%	PLD Level 3: 79%	PLD Level 2: 69%	PLD Level 1: 59%	
Distinguished command	Strong Command	Moderate Command	Partial Command	Little Command	
Student work shows distin-	Student work shows strong	Student work shows moderate	Student work shows partial	Student work shows little un-	
guished levels of understand-	levels of understanding of the	levels of understanding of the	understanding of the mathe-	derstanding of the mathemat-	
ing of the mathematics.	mathematics.	mathematics.	matics.	ics.	
Student constructs and com-	Student constructs and com-	Student constructs and com-	Student constructs and com-	Student attempts to constructs	
municates a complete response	municates a complete re-	municates a complete response	municates an incomplete re-	and communicates a response	
based on explana-	sponse based on explana-	based on explana-	sponse based on student's at-	using the:	
tions/reasoning using the:	tions/reasoning using the:	tions/reasoning using the:	tempts of explanations/ reason-	Tools:	
Tools:	Tools:	Tools:	ing using the:	 Manipulatives 	
 Manipulatives 	 Manipulatives 	 Manipulatives 	Tools:	 Five Frame 	
 Five Frame 	 Five Frame 	 Five Frame 	 Manipulatives 	 Ten Frame 	
 Ten Frame 	 Ten Frame 	 Ten Frame 	 Five Frame 	 Number Line 	
 Number Line 	 Number Line 	 Number Line 	 Ten Frame 	 Part-Part-Whole 	
 Part-Part-Whole 	 Part-Part-Whole 	 Part-Part-Whole 	 Number Line 	Model	
Model	Model	Model	 Part-Part-Whole 	Strategies:	
Strategies:	Strategies:	Strategies:	Model	 Drawings 	
 Drawings 	 Drawings 	 Drawings 	Strategies:	 Counting All 	
 Counting All 	 Counting All 	 Counting All 	 Drawings 	 Count On/Back 	
 Count On/Back 	 Count On/Back 	 Count On/Back 	 Counting All 	 Skip Counting 	
 Skip Counting 	 Skip Counting 	 Skip Counting 	 Count On/Back 	 Making Ten 	
 Making Ten 	 Making Ten 	 Making Ten 	 Skip Counting 	 Decomposing 	
• Decomposing	 Decomposing 	 Decomposing 	 Making Ten 	Number	
Number	Number	Number	 Decomposing 	Precise use of math vocab-	
Precise use of math vocab-	Precise use of math vocab-	• Precise use of math vocabu-	Number	ulary	
ulary	ulary	lary	Precise use of math vocab-		
Response includes an efficient			ulary	Response includes limited evi-	
and logical progression of	Response includes a logical	Response includes a logical but	Description in short	dence of the progression of	
mathematical reasoning and	progression of mathematical	incomplete progression of	Response includes an incom -	mathematical reasoning and	
understanding.	reasoning and understanding.	mathematical reasoning and	plete or illogical progression of	understanding.	
		understanding.	mathematical reasoning and		
E uninte	A mainta	Contains minor errors.	understanding.	1	
5 points	4 points	3 points	2 points	1 point	

DATA DRIVEN INSTRUCTION

Formative assessments inform instructional decisions. Taking inventories and assessments, observing reading and writing behaviors, studying work samples and listening to student talk are essential components of gathering data. When we take notes, ask questions in a student conference, lean in while a student is working or utilize a more formal assessment we are gathering data. Learning how to take the data and record it in a meaningful way is the beginning of the cycle.

Analysis of the data is an important step in the process. What is this data telling us? We must look for patterns, as well as compare the notes we have taken with work samples and other assessments. We need to decide what are the strengths and needs of individuals, small groups of students and the entire class. Sometimes it helps to work with others at your grade level to analyze the data.

Once we have analyzed our data and created our findings, it is time to make informed instructional decisions. These decisions are guided by the following questions:

- What mathematical practice(s) and strategies will I utilize to teach to these needs?
- What sort of grouping will allow for the best opportunity for the students to learn what it is I see as a need?
- Will I teach these strategies to the whole class, in a small guided group or in an individual conference?
- Which method and grouping will be the most effective and efficient? What specific objective(s) will I be teaching?

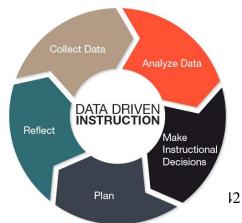
Answering these questions will help inform instructional decisions and will influence lesson planning.

Then we create our instructional plan for the unit/month/week/day and specific lessons.

It's important now to reflect on what you have taught.

Did you observe evidence of student learning through your checks for understanding, and through direct application in student work?

What did you hear and see students doing in their reading and writing?



Data Analysis Form	School:	Teacher:		Date:
Assessment:			NJSLS:	

GROUPS (STUDENT INITIALS)	SUPPORT PLAN	PROGRESS
MASTERED (86% - 100%) (PLD 4/5):		
DEVELOPING (67% - 85%) (PLD 3):		
INSECURE (51%-65%) (PLD 2):		
BEGINNING (0%-50%) (PLD 1):		

MATH PORTFOLIO EXPECTATIONS

The Student Assessment Portfolios for Mathematics are used as a means of documenting and evaluating students' academic growth and development over time and in relation to the NJSLS. The September task entry(ies) should reflect the prior year content and *can serve* as an additional baseline measure.

All tasks contained within the **Student Assessment Portfolios** should be aligned to NJSLS and be "practice forward" (closely aligned to the Standards for Mathematical Practice).

Four (4) or more additional tasks will be included in the **Student Assessment Portfolios** for Student Reflection and will be labeled as such.

K-2 GENERAL PORTFOLIO EXPECTATIONS:

- Tasks contained within the Student Assessment Portfolios are "practice forward" and denoted as "Individual", "Partner/Group", and "Individual w/Opportunity for Student Interviews¹.
- Each Student Assessment Portfolio should contain a "Task Log" that documents all tasks, standards, and rubric scores aligned to the performance level descriptors (PLDs).
- Student work should be attached to a completed rubric; with appropriate teacher feedback on student work.
- Students will have multiple opportunities to revisit certain standards. Teachers will capture each additional opportunity "as a new and separate score" in the task log.
- A 2-pocket folder for each Student Assessment Portfolio is recommended.
- All Student Assessment Portfolio entries should be scored and recorded as an Authentic Assessment grade (25%)².
- All Student Assessment Portfolios must be clearly labeled, maintained for all students, inclusive of constructive teacher and student feedback and accessible for review.

GRADES K-2

Student Portfolio Review

Provide students the opportunity to review and evaluate their portfolio at various points throughout the year; celebrating their progress and possibly setting goals for future growth. During this process, students <u>should</u> <u>retain ALL of their current artifacts</u> in their Mathematics Portfolio

2nd Grade Authentic Assessment #1 – High Jump Competition

High Jump Competition

Presley jumped 36 cm on her first jump in the high jump competition. On her second jump, she jumped 45 cm.

- a. How many total cm did Presley jump?
- b. How many fewer cm did Presley jump on her first jump than her second jump?

c. Logan also jumped twice. The total of Logan's two jumps was 95 cm. How many more total cm did Logan jump than Presley?

2.MD.5 : Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

Solution				
a. 81 cm b. 9 cm c. 14 cm	Level 4: Strong Com- mand	Level 3: Moderate Command	Level 2: Partial Command	Level 1: No Command
Student can an- swer both parts correctly.	Student can an- swer both parts correctly.	Student can only an- swer one part cor- rectly.	Student can only answer one part correctly.	Student can- not re- spond.
Clearly constructs and communicates a com- plete response based on explana- tions/reasoning using the: properties of operations relationship between addi- tion and sub- traction rela- tionship Response includes an efficient and logical progression of steps.	Clearly constructs and communicates a com- plete response for at least one part based on explanations/ reasoning using the: properties of operations relationship between addi- tion and sub- traction Response includes a logical progression of steps	Constructs and com- municates a complete response based on explana- tions/reasoning using the: properties of operations relationship between addi- tion and sub- traction Response includes a logical but incomplete progression of steps. Minor calculation er- rors	Constructs and communicates an incomplete re- sponse based on explana- tions/reasoning using the: properties of opera- tions relation- ship be- tween ad- dition and subtrac- tion Response includes an incomplete or Illogical progres- sion of steps.	The student shows no work or justification.

Core Instructional and Supplemental Materials (K-5)

EUREKA MATH V. 2019 (GREAT MINDS)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
K (v. 2019.)	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6
1	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6
2	 Teacher Edition: Module 1-8 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-8 Succeed Workbook Set: Module 1-8 Practice Workbook, Fluency: Module 1-8
3 4	 Teacher Edition: Module 1-7 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-7 Succeed Workbook Set: Module 1-7 Practice Workbook, Fluency: Module 1-7
5	 Teacher Edition: Module 1-7 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-7 Succeed Workbook Set: Module 1-7 Practice Workbook, Fluency: Module 1-7
	 Teacher Edition: Module 1-6 Eureka Math Teacher Resource Pack Eureka K-5 PD Toolkit 	 Learn Workbook Set: Module 1-6 Succeed Workbook Set: Module 1-6 Practice Workbook, Fluency: Module 1-6

MATH IN FOCUS v. 2015 (HOUGHTON MIFFLIN HARCOURT)

GRADE	TEACHER RESOURCES	STUDENT RESOURCES
К	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Set Teacher and Student Activity Cards Home -to- School Connection Book Online Teacher Technology Kit Big Book Set Online Interactive Whiteboard Lessons 	 Student Edition A – Pt. 1 Student Edition A – Pt. 2 Student Edition B – Pt. 1 Student Edition B – Pt. 2 Online Student Technology Kit
1	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Guide Reteaching Guide Home -to- School Connection Book Online Teacher Technology Kit Fact Fluency Online Interactive Whiteboard Lessons 	 Student Texts (A & B) Student Workbooks Online Student Technology Kit Student Interactivities
2-5	 Teacher Edition (A & B) Implementation Guide Assessment Package Enrichment Bundle Extra Practice Guide Transition Guides Reteaching Guide Home -to- School Connection Book Online Teacher Technology Kit Fact Fluency Online Interactive Whiteboard Lessons 	 Student Texts (A & B) Student Workbooks Online Student Technology Kit Student Interactivities

Supplemental Resources

Great Minds https://greatminds.org/

Embarc https://embarc.online/

Engage NY http://www.engageny.org/video-library?f[0]=im_field_subject%3A19

Common Core Tools http://commoncoretools.me/ http://www.ccsstoolbox.com/ http://www.achievethecore.org/steal-these-tools

Achieve the Core http://achievethecore.org/dashboard/300/search/6/1/0/1/2/3/4/5/6/7/8/9/10/11/12

Manipulatives

http://nlvm.usu.edu/en/nav/vlibrary.html

http://www.explorelearning.com/index.cfm?method=cResource.dspBrowseCorrelations&v=s&id=USA-000

http://www.thinkingblocks.com/

Illustrative Math Project : http://illustrativemathematics.org/standards/k8

Inside Mathematics: <u>http://www.insidemathematics.org/index.php/tools-for-teachers</u>

Sample Balance Math Tasks: <u>http://www.nottingham.ac.uk/~ttzedweb/MARS/tasks/</u>

Georgia Department of Education: https://www.georgiastandards.org/Common-Core/Pages/Math-K-5.aspx

Gates Foundations Tasks: http://www.gatesfoundation.org/college-ready-education/Documents/supporting-instruction-cards-math.pdf

References

"Eureka Math" Great Minds. 2018 < https://greatminds.org/account/products>